

$$f(x) = 9,000(0.66)^x$$

The given function  $f$  models the number of advertisements a company sent to its clients each year, where  $x$  represents the number of years since **1997**, and  $0 \leq x \leq 5$ . If  $y = f(x)$  is graphed in the  $xy$ -plane, which of the following is the best interpretation of the  $y$ -intercept of the graph in this context?

- A. The minimum estimated number of advertisements the company sent to its clients during the **5** years was **1,708**.
- B. The minimum estimated number of advertisements the company sent to its clients during the **5** years was **9,000**.
- C. The estimated number of advertisements the company sent to its clients in **1997** was **1,708**.
- D. The estimated number of advertisements the company sent to its clients in **1997** was **9,000**.

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The function  $g$  is defined by  $g(x) = x(x - 2)(x + 6)^2$ . The value of  $g(7 - w)$  is 0, where  $w$  is a constant. What is the sum of all possible values of  $w$ ?

$$p(t) = 90,000(1.06)^t$$

The given function  $p$  models the population of Lowell  $t$  years after a census. Which of the following functions best models the population of Lowell  $m$  months after the census?

A.  $r(m) = \frac{90,000}{12}(1.06)^m$

B.  $r(m) = 90,000\left(\frac{1.06}{12}\right)^m$

C.  $r(m) = 90,000\left(\frac{1.06}{12}\right)^{\frac{m}{12}}$

D.  $r(m) = 90,000(1.06)^{\frac{m}{12}}$

$$f(x) = (x + 7)^2 + 4$$

The function  $f$  is defined by the given equation. For what value of  $x$  does  $f(x)$  reach its minimum?

A right rectangular prism has a height of **9** inches. The length of the prism's base is  $x$  inches, which is **7** inches more than the width of the prism's base. Which function  $V$  gives the volume of the prism, in cubic inches, in terms of the length of the prism's base?

A.  $V(x) = x(x + 9)(x + 7)$

B.  $V(x) = x(x + 9)(x - 7)$

C.  $V(x) = 9x(x + 7)$

D.  $V(x) = 9x(x - 7)$

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$$f(x) = x^2 - 48x + 2,304$$

What is the minimum value of the given function?

The function  $g$  is defined by  $g(x) = (x + 14)(t - x)$ , where  $t$  is a constant. In the  $xy$ -plane, the graph of  $y = g(x)$  passes through the point  $(24, 0)$ . What is the value of  $g(0)$ ?

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The product of two positive integers is **462**. If the first integer is **5** greater than twice the second integer, what is the smaller of the two integers?

Two variables,  $x$  and  $y$ , are related such that for each increase of 1 in the value of  $x$ , the value of  $y$  increases by a factor of 4. When  $x = 0$ ,  $y = 200$ . Which equation represents this relationship?

A.  $y = 4^x$

B.  $y = 4^{200x}$

C.  $y = 200^x$

D.  $y = 200^{4x}$

$$f(t) = 8,000(0.65)^t$$

The given function  $f$  models the number of coupons a company sent to their customers at the end of each year, where  $t$  represents the number of years since the end of **1998**, and  $0 \leq t \leq 5$ . If  $y = f(t)$  is graphed in the  $ty$ -plane, which of the following is the best interpretation of the  $y$ -intercept of the graph in this context?

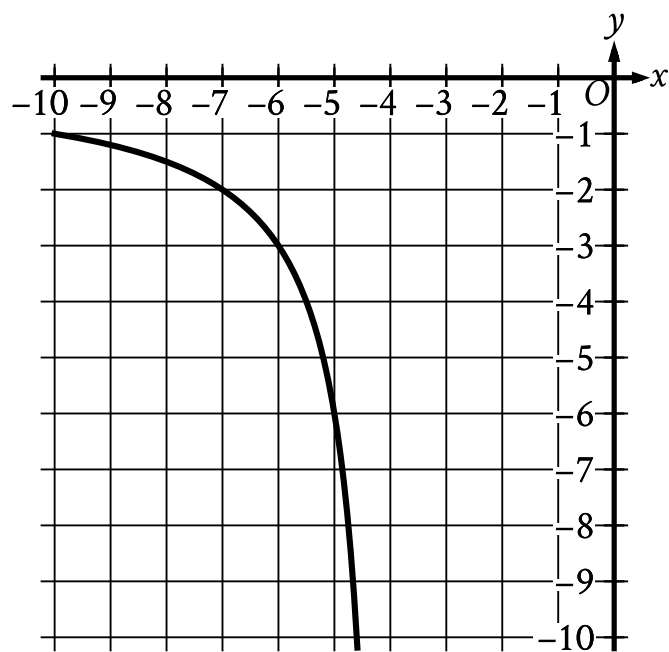
- A. The minimum estimated number of coupons the company sent to their customers during the **5** years was **1,428**.
- B. The minimum estimated number of coupons the company sent to their customers during the **5** years was **8,000**.
- C. The estimated number of coupons the company sent to their customers at the end of **1998** was **1,428**.
- D. The estimated number of coupons the company sent to their customers at the end of **1998** was **8,000**.

The function  $f$  is defined by  $f(x) = (-8)(2)^x + 22$ . What is the  $y$ -intercept of the graph of  $y = f(x)$  in the  $xy$ -plane?

- A.  $(0, 14)$
- B.  $(0, 2)$
- C.  $(0, 22)$
- D.  $(0, -8)$

$$y = x^2 - 14x + 22$$

The given equation relates the variables  $x$  and  $y$ . For what value of  $x$  does the value of  $y$  reach its minimum?



The rational function  $f$  is defined by an equation in the form  $f(x) = \frac{a}{x+b}$ , where  $a$  and  $b$  are constants. The partial graph of  $y = f(x)$  is shown. If  $g(x) = f(x+4)$ , which equation could define function  $g$ ?

- A.  $g(x) = \frac{6}{x}$
- B.  $g(x) = \frac{6}{x+4}$
- C.  $g(x) = \frac{6}{x+8}$
- D.  $g(x) = \frac{6(x+4)}{x+4}$

A model estimates that at the end of each year from **2015** to **2020**, the number of squirrels in a population was **150%** more than the number of squirrels in the population at the end of the previous year. The model estimates that at the end of **2016**, there were **180** squirrels in the population. Which of the following equations represents this model, where  $n$  is the estimated number of squirrels in the population  $t$  years after the end of **2015** and  $t \leq 5$ ?

A.  $n = 72^t$

B.  $n = 72^{5-t}$

C.  $n = 180^t$

D.  $n = 180^{5-t}$

$$f(x) = 9(4)^x$$

The function  $f$  is defined by the given equation. If  $g(x) = f(x + 2)$ , which of the following equations defines the function  $g$ ?

A.  $g(x) = 18(4)^x$

B.  $g(x) = 144(4)^x$

C.  $g(x) = 18(8)^x$

D.  $g(x) = 81(16)^x$

$$f(x) = (x - 10)(x + 13)$$

The function  $f$  is defined by the given equation. For what value of  $x$  does  $f(x)$  reach its minimum?

A.  $-130$

B.  $-13$

C.  $-\frac{23}{2}$

D.  $-\frac{3}{2}$

In the  $xy$ -plane, a parabola has vertex  $(9, -14)$  and intersects the  $x$ -axis at two points. If the equation of the parabola is written in the form  $y = ax^2 + bx + c$ , where  $a$ ,  $b$ , and  $c$  are constants, which of the following could be the value of  $a + b + c$ ?

A.  $-23$

B.  $-19$

C.  $-14$

D.  $-12$

$$f(x) = (1.84)^{\frac{x}{4}}$$

The function  $f$  is defined by the given equation. The equation can be rewritten as  $f(x) = \left(1 + \frac{p}{100}\right)^x$ , where  $p$  is a constant. Which of the following is closest to the value of  $p$ ?

- A. 16
- B. 21
- C. 46
- D. 96

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For the function  $f$ ,  $f(0) = 86$ , and for each increase in  $x$  by 1, the value of  $f(x)$  decreases by 80%. What is the value of  $f(2)$ ?

$$f(x) = (x - 1)(x + 3)(x - 2)$$

In the  $xy$ -plane, when the graph of the function  $f$ , where  $y = f(x)$ , is shifted up  $6$  units, the resulting graph is defined by the function  $g$ . If the graph of  $y = g(x)$  crosses through the point  $(4, b)$ , where  $b$  is a constant, what is the value of  $b$ ?

For the function  $q$ , the value of  $q(x)$  decreases by 45% for every increase in the value of  $x$  by 1. If  $q(0) = 14$ , which equation defines  $q$ ?

A.  $q(x) = 0.55(14)^x$

B.  $q(x) = 1.45(14)^x$

C.  $q(x) = 14(0.55)^x$

D.  $q(x) = 14(1.45)^x$

The function  $f$  is defined by  $f(x) = a\sqrt{x+b}$ , where  $a$  and  $b$  are constants. In the  $xy$ -plane, the graph of  $y = f(x)$  passes through the point  $(-24, 0)$ , and  $f(24) < 0$ . Which of the following must be true?

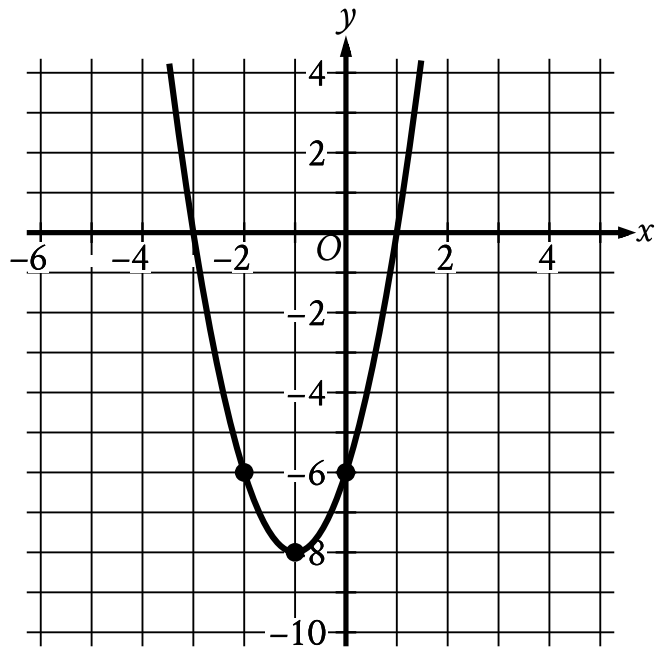
- A.  $f(0) = 24$
- B.  $f(0) = -24$
- C.  $a > b$
- D.  $a < b$

When the quadratic function  $f$  is graphed in the  $xy$ -plane, where  $y = f(x)$ , its vertex is  $(-3, 6)$ . One of the  $x$ -intercepts of this graph is  $(-\frac{17}{4}, 0)$ . What is the other  $x$ -intercept of the graph?

- A.  $(-\frac{29}{4}, 0)$
- B.  $(-\frac{7}{4}, 0)$
- C.  $(\frac{5}{4}, 0)$
- D.  $(\frac{17}{4}, 0)$

| $x$ | $y$ |
|-----|-----|
| 21  | -8  |
| 23  | 8   |
| 25  | -8  |

The table shows three values of  $x$  and their corresponding values of  $y$ , where  $y = f(x) + 4$  and  $f$  is a quadratic function. What is the  $y$ -coordinate of the  $y$ -intercept of the graph of  $y = f(x)$  in the  $xy$ -plane?



The graph of  $y = 2x^2 + bx + c$  is shown, where  $b$  and  $c$  are constants. What is the value of  $bc$ ?

A machine launches a softball from ground level. The softball reaches a maximum height of **51.84** meters above the ground at **1.8** seconds and hits the ground at **3.6** seconds. Which equation represents the height above ground  $h$ , in meters, of the softball  $t$  seconds after it is launched?

A.  $h = -t^2 + 3.6$

B.  $h = -t^2 + 51.84$

C.  $h = -16t^{\text{msup}} - 3.6$

D.  $h = -16t^{\text{msup}} + 51.84$

$$y = 576^{(2x+2)}$$

The graph of the given equation in the  $xy$ -plane has a  $y$ -intercept of  $(r, s)$ . Which of the following equivalent equations displays the value of  $s$  as a constant, a coefficient, or the base?

A.  $y = \text{msup}$

B.  $y = \text{msup}$

C.  $y = \frac{1}{24} \text{msup}$

D.  $y = \frac{1}{576} \text{msup}$

The function  $f$  is defined by  $f(x) = a^x + b$ , where  $a$  and  $b$  are constants. In the  $xy$ -plane, the graph of  $y = f(x)$  has an  $x$ -intercept at  $(2, 0)$  and a  $y$ -intercept at  $(0, -323)$ . What is the value of  $b$ ?

| $x$   | $g(x)$ |
|-------|--------|
| $-27$ | $3$    |
| $-9$  | $0$    |
| $21$  | $5$    |

The table shows three values of  $x$  and their corresponding values of  $g(x)$ , where  $g(x) = \frac{f(x)}{x+3}$  and  $f$  is a linear function. What is the  $y$ -intercept of the graph of  $y = f(x)$  in the  $xy$ -plane?

- A.  $(0, 36)$
- B.  $(0, 12)$
- C.  $(0, 4)$
- D.  $(0, -9)$

$$f(x) = 272(2)^x$$

The function  $f$  is defined by the given equation. If  $h(x) = f(x - 4)$ , which of the following equations defines function  $h$ ?

A.  $h(x) = 17(2)^x$

B.  $h(x) = 68(2)^x$

C.  $h(x) = 272(16)^x$

D.  $h(x) = 272(8)^x$

The functions  $f$  and  $g$  are defined by the given equations, where  $x \geq 0$ . Which of the following equations displays, as a constant or coefficient, the maximum value of the function it defines, where  $x \geq 0$ ?

I.  $f(x) = 33(0.4)^{x+3}$

II.  $g(x) = 33(0.16)(0.4)^{x-2}$

- A. I only
- B. II only
- C. I and II
- D. Neither I nor II

The function  $f(x) = \frac{1}{9}(x - 7)^2 + 3$  gives a metal ball's height above the ground  $f(x)$ , in inches,  $x$  seconds after it started moving on a track, where  $0 \leq x \leq 10$ . Which of the following is the best interpretation of the vertex of the graph of  $y = f(x)$  in the  $xy$ -plane?

- A. The metal ball's minimum height was **3** inches above the ground.
- B. The metal ball's minimum height was **7** inches above the ground.
- C. The metal ball's height was **3** inches above the ground when it started moving.
- D. The metal ball's height was **7** inches above the ground when it started moving.

A quadratic function models the height, in feet, of an object above the ground in terms of the time, in seconds, after the object is launched off an elevated surface. The model indicates the object has an initial height of **10** feet above the ground and reaches its maximum height of **1,034** feet above the ground **8** seconds after being launched. Based on the model, what is the height, in feet, of the object above the ground **10** seconds after being launched?

- A. **234**
- B. **778**
- C. **970**
- D. **1,014**

$$P(t) = 260(1.04)^{\left(\frac{6}{4}\right)t}$$

The function  $P$  models the population, in thousands, of a certain city  $t$  years after **2003**. According to the model, the population is predicted to increase by **4%** every  $n$  months. What is the value of  $n$ ?

- A. **8**
- B. **12**
- C. **18**
- D. **72**

$$P(t) = 290(1.04)^{\left(\frac{4}{6}\right)t}$$

The function  $P$  models the population, in thousands, of a certain city  $t$  years after **2005**. According to the model, the population is predicted to increase by  $n\%$  every **18** months. What is the value of  $n$ ?

A. **0.38**

B. **1.04**

C. **4**

D. **6**

$$f(x) = 4x^2 - 50x + 126$$

The given equation defines the function  $f$ . For what value of  $x$  does  $f(x)$  reach its minimum?

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The function  $f$  is defined by  $f(x) = (x - 6)(x - 2)(x + 6)$ . In the  $xy$ -plane, the graph of  $y = g(x)$  is the result of translating the graph of  $y = f(x)$  up 4 units. What is the value of  $g(0)$ ?

The first term of a sequence is **9**. Each term after the first is **4** times the preceding term. If ***w*** represents the ***n***th term of the sequence, which equation gives ***w*** in terms of ***n***?

A.  $w = 4(9^n)$

B.  $w = 4(9^{n-1})$

C.  $w = 9(4^n)$

D.  $w = 9(4^{n-1})$

At the time that an article was first featured on the home page of a news website, there were 40 comments on the article. An exponential model estimates that at the end of each hour after the article was first featured on the home page, the number of comments on the article had increased by 190% of the number of comments on the article at the end of the previous hour. Which of the following equations best represents this model, where  $C$  is the estimated number of comments on the article  $t$  hours after the article was first featured on the home page and  $t \leq 4$ ?

A.  $C = 40^{1.9t}$

B.  $C = 40^{1.9t}$

C.  $C = 40^{1.9t}$

D.  $C = 40^{1.9t}$

Function  $f$  is defined by  $f(x) = -a^x + b$ , where  $a$  and  $b$  are constants. In the  $xy$ -plane, the graph of  $y = f(x) - 15$  has a  $y$ -intercept at  $(0, -\frac{99}{7})$ . The product of  $a$  and  $b$  is  $\frac{65}{7}$ . What is the value of  $a$ ?

Function  $f$  is defined by  $f(x) = (x + 6)(x + 5)(x + 1)$ . Function  $g$  is defined by  $g(x) = f(x - 1)$ . The graph of  $y = g(x)$  in the  $xy$ -plane has  $x$ -intercepts at  $(a, 0)$ ,  $(b, 0)$ , and  $(c, 0)$ , where  $a$ ,  $b$ , and  $c$  are distinct constants. What is the value of  $a + b + c$ ?

A.  $-15$

B.  $-9$

C.  $11$

D.  $15$

For the exponential function  $f$ , the value of  $f(1)$  is  $k$ , where  $k$  is a constant. Which of the following equivalent forms of the function  $f$  shows the value of  $k$  as the coefficient or the base?

A.  $f(x) = 50(2)^{x+1}$

B.  $f(x) = 80(2)^x$

C.  $f(x) = 128(2)^{x-1}$

D.  $f(x) = 205(2)^{x-2}$

$$f(x) = |59 - 2x|$$

The function  $f$  is defined by the given equation. For which of the following values of  $k$  does  $f(k) = 3k$ ?

- A.  $\frac{59}{5}$
- B.  $\frac{59}{2}$
- C.  $\frac{177}{5}$
- D. 59

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A rectangle has an area of **155** square inches. The length of the rectangle is **4** inches less than **7** times the width of the rectangle. What is the width of the rectangle, in inches?

$$f(x) = ax^2 + 4x + c$$

In the given quadratic function,  $a$  and  $c$  are constants. The graph of  $y = f(x)$  in the  $xy$ -plane is a parabola that opens upward and has a vertex at the point  $(h, k)$ , where  $h$  and  $k$  are constants. If  $k < 0$  and  $f(-9) = f(3)$ , which of the following must be true?

I.  $c < 0$

II.  $a \geq 1$

A. I only

B. II only

C. I and II

D. Neither I nor II

Function  $f$  is defined by  $f(x) = -a^x + b$ , where  $a$  and  $b$  are constants. In the  $xy$ -plane, the graph of  $y = f(x) - 12$  has a  $y$ -intercept at  $(0, -\frac{75}{7})$ . The product of  $a$  and  $b$  is  $\frac{320}{7}$ . What is the value of  $a$ ?

$$f(x) = 5,470(0.64)^{\frac{x}{12}}$$

The function  $f$  gives the value, in dollars, of a certain piece of equipment after  $x$  months of use. If the value of the equipment decreases each year by  $p\%$  of its value the preceding year, what is the value of  $p$ ?

- A. 4
- B. 5
- C. 36
- D. 64

$$f(x) = (x - 14)(x + 19)$$

The function  $f$  is defined by the given equation. For what value of  $x$  does  $f(x)$  reach its minimum?

A.  $-266$

B.  $-19$

C.  $-\frac{33}{2}$

D.  $-\frac{5}{2}$

The functions  $f$  and  $g$  are defined by the given equations.

$$f(x) = 3 + |-2x - x^2|$$

$$g(w) = \left| \frac{-w}{w-1} \right| - w + 5$$

If  $f(-4) = c$ , where  $c$  is a constant, what is the value of  $g(c)$ ?

The function  $h$  is defined by  $h(x) = a^x + b$ , where  $a$  and  $b$  are positive constants. The graph of  $y = h(x)$  in the  $xy$ -plane passes through the points  $(0, 10)$  and  $(-2, \frac{325}{36})$ . What is the value of  $ab$ ?

- A.  $\frac{1}{4}$
- B.  $\frac{1}{2}$
- C. **54**
- D. **60**

Square P has a side length of  $x$  inches. Square Q has a perimeter that is **176** inches greater than the perimeter of square P. The function  $f$  gives the area of square Q, in square inches. Which of the following defines  $f$ ?

A.  $f(x) = (x + 44)^2$

B.  $f(x) = (x + 176)^2$

C.  $f(x) = (176x + 44)^2$

D.  $f(x) = (176x + 176)^2$

$$f(x) = 4x^2 + 64x + 262$$

The function  $g$  is defined by  $g(x) = f(x + 5)$ . For what value of  $x$  does  $g(x)$  reach its minimum?

A.  $-13$

B.  $-8$

C.  $-5$

D.  $-3$

Which of the following functions has(have) a minimum value at  $-3$ ?

I.  $f(x) = -6(3)^x - 3$

II.  $g(x) = -3(6)^x$

- A. I only
- B. II only
- C. I and II
- D. Neither I nor II

The function  $f$  is defined by  $f(x) = ax^2 + bx + c$ , where  $a$ ,  $b$ , and  $c$  are constants. The graph of  $y = f(x)$  in the  $xy$ -plane passes through the points  $(7, 0)$  and  $(-3, 0)$ . If  $a$  is an integer greater than 1, which of the following could be the value of  $a + b$ ?

- A.  $-6$
- B.  $-3$
- C.  $4$
- D.  $5$

A quadratic function models a projectile's height, in meters, above the ground in terms of the time, in seconds, after it was launched. The model estimates that the projectile was launched from an initial height of **7** meters above the ground and reached a maximum height of **51.1** meters above the ground **3** seconds after the launch. How many seconds after the launch does the model estimate that the projectile will return to a height of **7** meters?

- A. **3**
- B. **6**
- C. **7**
- D. **9**